Data Representation

Number bases

Denary (or decimal) is base-10 and is the number system we are most familiar with. We have the columns of units, tens, hundreds, thousands and so on. Base-10 means that we have 10 possible values (0, 1, 2, 3, 4, 5, 6, 7, 8, 9) in each column.

Binary is base-2 and has 2 values, 0 and 1. It requires a greater number of digits in binary to represent a number than denary. This is how data and instructions are stored in a computer.

To calculate the maximum value for a given number of bits we use 2ⁿ-1 where n is the number of bits. For example for 4 bits we have 2^4 -1 which is 15.

Bits	Max value binary	Max value denary
1	12	110
2	112	310
3	1112	710
4	11112	1510
5	111112	3110
6	1111112	63 ₁₀
7	11111112	127 ₁₀
8	11111111 ₂	25510

Hexadecimal is base-16. To make up the 16 values we use the ten denary numbers in addition to 6 letters (A, B, C, D, E, F).

Denary	Hex.	Binary	Denary	Hex.	Binar
D ₁₀	016	00002	810	816	1000 ₂
1 10	116	00012	910	9 ₁₆	1001 ₂
210	216	00102	1010	A ₁₆	1010 ₂
3 10	316	00112	1110	B ₁₆	1011 ₂
410	416	01002	1210	C ₁₆	11002
510	516	01012	1310	D ₁₆	11012
610	616	01102	1410	E ₁₆	11102
710	716	01112	1510	F ₁₆	11112

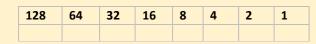
Hexadecimal is used a lot in computing because it much easier to read than binary. There are far fewer characters than binary. So hexadecimal is often used in place of binary as a shorthand to save space. For instance, the hexadecimal number 7BA3D456 (8 digits) is 0111101110100011110100010101010 (32 digits) in binary which is hard to read.

Hexadecimal is better than denary at representing binary because hexadecimal is based on powers of 2.

Converting between number bases

Denary to binary conversion

1. Create a grid:



2. Add a 1 to the corresponding cell if number contributes to target number and 0 to all the other cells

Worked example: convert 24₁₀ to binary.

128	64	32	16	8	4	2	1
0	0	0	1	1	0	0	0

1610 + 810=2410

The binary value is 11000₂ (we can ignore the preceding zeros)

Binary to denary conversion

Worked example: Convert 01011001₂ to denary 1. Create the grid:

128	64	32	16	8	4	2	1
0	1	0	1	1	0	0	1

2. Add up the cells that have a corresponding value of 1: $64 + 16_{10} + 8_{10} + 1 = 89_{10}$

Hexadecimal to denary conversion

- 1) Convert the two hex values separately to denary value
- 2) Multiply the first value by 16
- 3) Add the second value

Worked example: Covert A316 to denary $A_{16} = 10_{10}$ $3_{16} = 3_{10}$

 $(10_{10} \times 16_{10}) + 3_{10} = 163_{10}$

Denary to hexadecimal conversion

- 1) Integer divide the denary number by 16
- 2) Take the modulus 16 of the denary number
- 3) Convert the two numbers to the corresponding hex values.

Worked example: Convert 18910 to hex

$189_{10} / 16_{10} = 11_{10}$ remainder 15_{10}
$11_{10} = B_{16}$
15 ₁₀ = F ₁₆
189 ₁₀ = <u>BF₁₆</u>

Hexadecimal to binary conversion

- 1. Find the corresponding 4-bit binary number for the two numbers
- 2. Concatenate the two binary values to give the final binary value

*Example: convert C3*¹⁶ *to binary* $C_{16} = 12_{10} = 1100_2$ $3_{16} = 3_{10} = 0011_2$ 110000112

Binary to hexadecimal conversion

- 1. Split the binary number into groups of 4 bits: 11102 10102
- 2. Find the corresponding Hex value for each of the 4-bit groups

Worked example: Convert 111010102 to hexadecimal

 $1110_2 = 14_{10} = E_{16}$ $1010_2 = 10_{10} = A_{16}$

Units of Information

Unit	Symbol	Number of bytes
Kilobyte	КВ	10 ³ (1000)
Megabyte	MB	10 ⁶ (1 million)
Gigabyte	GB	10 ⁹ (1 billion)
Terabyte	ТВ	10 ¹² (1 trillion)

either 0 or 1.

1 byte = 8 bits 1 nibble = 4 bits

Low
Upp
Nur
Syn
Cor

A
А
В
а
b
"0"
"1"

- platforms.
- Japanese, Emojis etc.

Binary addition rules	Example
$0_{2} + 0_{2} = 0_{2}$ $0_{2} + 1_{2} = 1_{2}$ $1_{2} + 0_{2} = 1_{2}$ $1_{2} + 1_{2} = 10_{2} (carry 1)$ $1_{2} + 1_{2} + 1_{2} = 11_{2} (carry 1)$	$ \begin{array}{r} 10101001_{2} \\ 00001001_{2} \\ + \\ \underline{00010101}_{2} \\ \underline{11000111}_{2} \\ \text{carry 111 1} \end{array} $

by powers of 2

multiply/divide							
shift	<<4	<<3	<<2	<<1	>>1	>>2	>>3

Example: Apply shift operator to 1101₂ (13₁₀)

Shift	Result	denary
<<1	110102	13 ₁₀ x 2 ₁₀ = 26 ₁₀
<<2	1101002	13 ₁₀ x 4 ₁₀ = 52 ₁₀
>>1	110	13_{10} // 2_{10} = 6_{10}

shift operator is applied.

11102 | 10102 <u>EA16</u>

A bit is the fundamental unit of binary numbers. A bit is a binary digit that can be

Character Encoding

Character coding schemes allows text to be represented in the computer. One such coding scheme is ASCII. ASCII uses 7 bits to represent each character which means that a total of 128 characters can be represented.

ver case letters	26
per case letters	26
mbers	10
nbols (e.g. comma, colon)	33
ntrol characters	33

ASCII encoded values for some characters

2		
	10000012	6510
	10000102	6610
	1100001 ₂	97 ₁₀
	1100010 ₂	9810
	0110000 ₂	4810
	0110001 ₂	49 10

ASCII has a limited character set (7 bits, 128 characters), but Unicode has 16 bits and allows many more (65K) characters.

Unicode provides a unique character for different languages and different

It allows us to represent different alphabets for instance Greek, Mandarin,

Unicode and ASCII are the same up to 127.

Binary a	ddition
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Binary Shift

The binary shift operator is used to perform multiplication and division of numbers

Note that odd numbers are rounded down to the nearest integer when the right